

GENERALIZE ROLE OF THE HYPERGEOMETRIC FUNCTION OF MULTIVARIATE MATRIX ARGUMENT IN THE WIRELESS COMMUNICATIONS

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Abstract: *Premature complications in wireless transmission: Signal lack allocated to building, ground, etc. logically happening "noise" in addition cause signal to become lighter in communication. The use of numerous antennas led to considerable increase in sequence transfer. Matrix assumption has set up lots of application in physics, statistics, mathematics, bio matrix, animation and engineering since its inception. even though early developments were stimulated by realistic investigational effort, random matrices are at the moment second-hand in fields as various as Riemann hypothesis, stochastic differential equations, packed together matter physics, statistical physics, chaotic systems, numerical linear algebra, neural networks, multivariate statistics, in sequence theory, signal handing out and small-world, networks. This editorial provides a lesson on random matrices which provide a general idea of the theory and bring collectively in one foundation the most important grades in recent times obtained. in addition, the submission of random matrix theory to the basic limits of wireless communication channels is described in depth. The exploit of various antenna for transmit and acceptance wireless communications signal*

The major development in wireless communications systems

- *enlarged records throughput*
- *Longer link range*
- *No need for supplementary bandwidth or broadcast authority*
- *Higher supernatural effectiveness (hertz of bandwidth)*
- *Reduced fading.*

I. INTRODUCTION

BEGINNING its commencement, random matrix supposition has been profoundly inclined by its application in physics, statistics and engineering. The landmark Contributions to the theory of random matrices of Wishart (1928) [311], was motivated to a outsized amount by practical investigational problems. Random matrix theory with exacting highlighting on asymptotic theorems on the allocation of Eigen values and extraordinary values beneath a variety of assumption on the combined delivery of the random matrix entries. While results for matrices with fixed magnitude are frequently weighty and offer partial close by, as the matrices mature large with a agreed aspect ratio. a number of authoritative and pleasing theorems make certain convergence of the experimental Eigen value distributions to deterministic

functions. The organization of this monograph is the following. Introduce the universal class of vector channel of interest in wireless communications. These channels are categorized by random matrices. That admits various arithmetic metaphors depending on the actual application. Motivates interest in large random matrix theory by focus on two presentation method of engineering curiosity: Shannon capacity and linear minimum mean-square error, which are resolute by the allocation of the remarkable principles of the channel matrix.

II. MATERIAL AND METHODS

A. Wireless Channels

The most recent decade has witnessed a regeneration in the in sequence theory of wireless communication channels. Two prime reasons for the well-built level of movement in this ground can be recognized. The initial is the increasing significance of the well-organized utilizes of bandwidth and authority in view of the mounting stipulate for wireless services. The moment is the piece of in sequence that some of the major challenges in the learn of the faculty of wireless channels have merely be profitably tackled a moment ago. Fading, wideband, multiuser and multi-antenna are some of the key features that characterize wireless channels of contemporary interest. Most of the information theoretic creative writing that studies the effect of those features on channel aptitude deal with linear vector recollection less channels of the form

$$u = Hv + n \quad (1)$$

$$\frac{1}{N} I(x; y|H) = \frac{1}{N} \log \det(I +_{SNR} HH^+)$$

Where v is the K -dimensional input vector, u is the N -dimensional output vector, and the N -dimensional vector n models the additive circularly symmetric Gaussian noise. All these quantities are, in general, Complex-valued. In addition to input constraint, and the degree of awareness of the channel at receiver and transmitter, (1) is characterized by the distribution of the $N \times K$ random channel matrix H whose entries are also complex-valued..

B. The Role of the Singular Values

Pretentious that the channel matrix H is entirely recognized at the recipient, the capability of (1) beneath contribution authority constraints depends on the sharing of the remarkable values of H . We heart in the simplest location to demonstrate this direct as crisply as potential: understand that the entries of the contribution vector u .

For example, this is the case in a synchronous DS-CDMA multi-access channel or for a single-user multi-antenna channel where the satellite dish cannot pathway the channel. The experiential collective distribution function of the Eigen values of an $n \times n$ Hermitian matrix A is denoted by F_A^n .

$$F_A^n(x) = \frac{1}{n} \sum_{i=1}^n 1\{\lambda_i(A) \leq x\}, \quad (2)$$

Everywhere $\lambda_1(A) \dots \lambda_n(A)$ are the Eigen values of A and $1\{\cdot\}$ is the indicator function.

At present, judge a subjective $N \times K$ matrix H . Since the nonzero singular values of H and H^\dagger are indistinguishable, we be able to write

$$NF_{HH^+}^N(x) - Nu(x) = KF_{HH^+}^K(x) - Ku(x) \quad (3)$$

Where $u(x)$ is the unit-step function ($u(x) = 0, x \leq 0; u(x) = 1, x > 0$). Gaussian input, the normalized input-output mutual information of (1) conditioned on H

$$\begin{aligned} &= \frac{1}{N} \sum_{i=1}^N \log(1 + SNR \lambda_i(HH^+)) \\ &= \int_0^\infty \log(1 + SNRx) dF_{HH^+}^N(x) \end{aligned} \quad (4)$$

With the transmitted signal-to-noise ratio

$$SNR = \frac{NE \left\| X \right\|^2}{KE \left\| X \right\|^2} \quad (5)$$

and with $\lambda_i(HH^\dagger)$ equivalent to the i th squared singular value of H . If the channel is acknowledged at the receiver and its dissimilarity over time is stationary and ergodic, then the anticipation of (4) over the division of H is the channel capability. Further in general, the allocation of the random variable (4) determines the outage capacity.

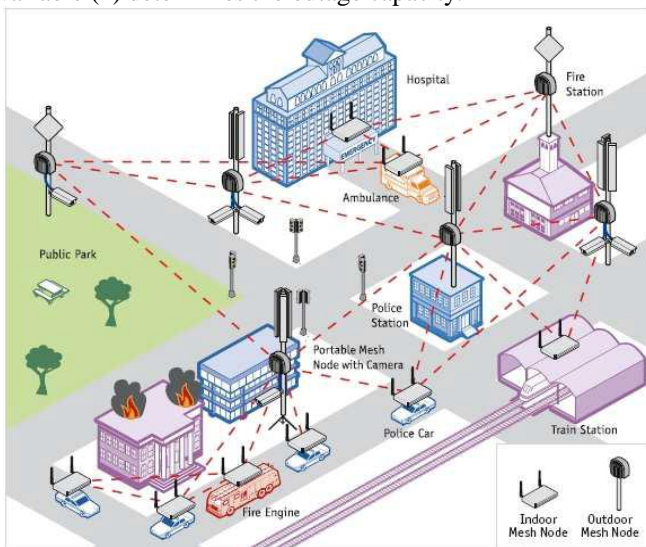


Figure 1

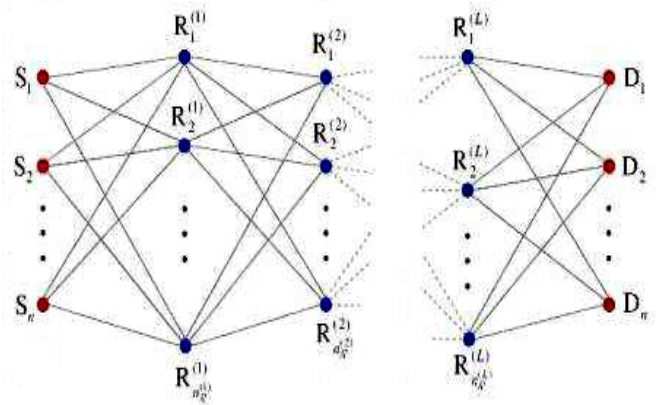


Figure 2

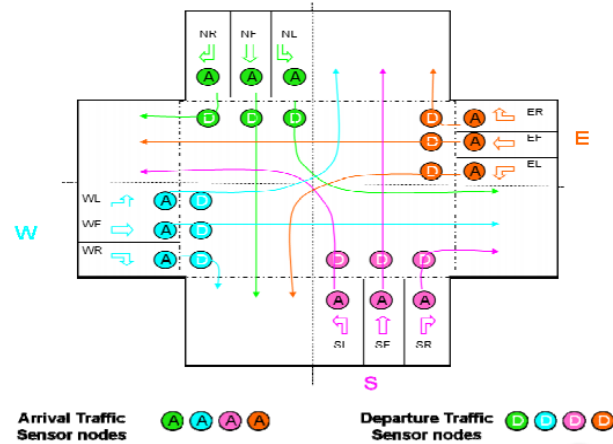


Figure 3

C. Multiple-Input Multiple-Output (MIMO) communications system

MIMO system: The use of multiple antennas for transmitting and receiving wireless communications signals. Signal transmission

- nt: The number of transmitting antennas
- nr: The number of receiving antennas
- x: The $nt \times 1$ vector of signals sent by the transmitting antennas
- y: The $nr \times 1$ vector of signals arriving at the receiving antennas

Both x and y are vectors of complex numbers
 We assume, w.l.o.g., that $nr \geq nt$
 Channel matrix: $A = nr \times nt$ complex random matrix, G , relating x and y

D. Shannon: Information theory:

Channel capacity: "The tightest upper bound on the amount of information that can be transmitted reliably over a communications channel." Channel capacity is measured in "nats" (natural units for information entropy):

$$1nat = 1 / \log 2 \approx 1.44bits$$

For MIMO models, the channel capacity is

$$I(x, \epsilon | G) = \log \det(I + G^* G)$$

Here $G^* = G^\dagger$ is adjoint of G .

Average channel capacity: The average amount of

information that can be transmitted by the channel. Engineers wish to calculate the average channel capacity. We need to calculate $EI(x, \varepsilon|G)$ with respect to the probability distribution of G, x , and ε

Calculate the moment-generating function of $I(x, \varepsilon|G)$:

$$E(e^{zI(x, \varepsilon|G)}), z \in \mathbb{C}$$

and then compute the first moment in the usual way:

$$EI(x, \varepsilon|G) = \frac{\partial}{\partial z} E(e^{zI(x, \varepsilon|G)}) \Big|_{z=0}$$

$$I(x, \varepsilon|G) = \log \det(I + G * G)$$

$$E(e^{zI(x, \varepsilon|G)}) = E \det(I + G * G)^z$$

G has i.i.d. CN (0, 1)-distributed components, so

$$E \det(I + G * G)^z \propto \int_{\mathbb{C}^{n_r \times n_t}} \det(I + G * G)^z e^{-trG * G} dG$$

$G \in \mathbb{C}^{n_r \times n_t}$ has a complex Wishart distribution, so we can transform the integral into a Selberg integral over the Eigen values of $G \in \mathbb{C}^{n_r \times n_t}$

$$E \det(I + G * G)^z \propto \int_{\mathbb{R}^{n_t}} \prod_{j < k} (\lambda_j - \lambda_k)^2 \prod_{k=1}^{n_t} (1 + \lambda_k)^z \lambda_k^{n_t - n_r} e^{-\lambda_k} d\lambda_k$$

Or, by changing variables to a Hermitian positive definite matrix $H = G \in \mathbb{C}^{n_r \times n_t}$, we obtain

$$E \det(I + G * G)^z \propto \int_{H > 0} \det(I + H)^z \det(H)^{n_t - n_r} e^{-trH} dH$$

This integral is a confluent hyper geometric function of matrix argument:

$$E \det(I + G * G)^z \propto \alpha \psi(n_t; z + n_t; I)$$

III. RESULT AND DISCUSSION

The hyper geometric function of Hermitian matrix argument spoken as ratios of determinants of traditional hyper geometric functions. The ratios-of-determinant formulas had been derived earlier. Using these results, the wireless communications community ultimately were able to get hold of exact formulas for typical channel capacity

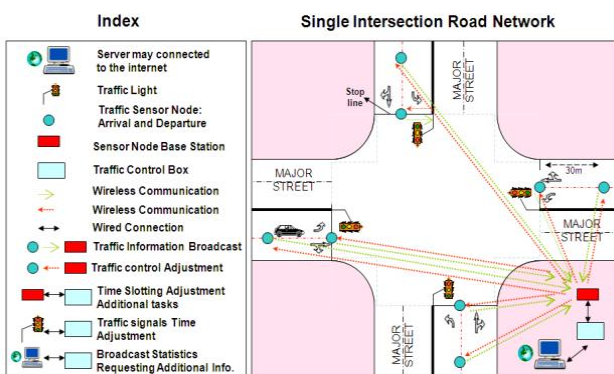


Figure 4

In this paper, the plan of an intellectual traffic control system, utilizing and efficiently organization WSNs, is obtainable. An adaptive traffic indication time manipulation algorithm based on an original traffic infrastructure using WSNs is planned on a single and several road intersections. A new technique for changing the traffic phase's sequence, during the traffic control, is an additional involvement of this paper. The designed classification with its surrounded algorithms is proved to play a major role in alleviating the congestion problem when compared to ineffective classical traffic control systems. Additionally, our traffic control system can be with no trouble installed and attached to the existing traffic road infrastructure at a low cost and within a reasonable time. The system is self-configuring and operates in real-time to detect traffic states and exchange information with other nodes via a wireless communication with self-recovery function. In addition, no traffic disruption will be obligatory when a new traffic antenna (sensor) is to be installed. In the future work of this study, we plan to simulate the human driving behaviors and enclose the entire system using technology. In addition, different types of intersections and different types of crossing directions in the system will be considered.

REFERENCES

- [1] Sharma Yogesh (2013), Solution of Integral Equation of Matrix Variable Involving Laguerre Function, International Journal of Scientific Research and Reviews, 2(1)Suppl.01-06
- [2] A.K. Vyas, Some Generalized Multivariate G – Function Distribution of Matrix Argument and Statistical Properties and Integral Transform, IJIRSE
- [3] Minnesota Department of Transportation, “Portable non-intrusive traffic detection system,” <http://www3.dot.state.mn.us/guidestar/pdf/pnitsds/techmemo-axlebased.pdf>.
- [4] S. Coleri, S. Y. Cheung, and P. Varaiya, “Sensor networks for monitoring traffic,” in Proceedings of the 42nd Annual Allerton Conference on Communication, Control, and Computing, 2004, pp. 32-40.
- [5] Greater Amman Municipality, “Traffic report study 2007,” <http://www.ammancity.gov.jo/arabic/docs/GAM4-2007.pdf>.
- [6] The Vehicle Detector Clearinghouse, “A summary of vehicle detection and surveillance technologies used in intelligent transportation systems,” Southwest Technology Development Institute, 2000.
- [7] I. F. Akyildiz, W. Su, Y. Sankarasubramaniam, and E. Cayirci, “A survey on sensor networks,” IEEE Communications Magazine, Vol. 40, 2002, pp. 102-114.
- [8] A. N. Knaian, “A wireless sensor network for smart roadbeds and intelligent transportation systems,” Technical Report, Electrical Science and

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- Engineering, Massachusetts Institute of Technology, June 2000.
- [9] W. J. Chen, L. F. Chen, Z. L. Chen, and S. L. Tu, "A real-time dynamic traffic control system based on wireless sensor network," in Proceedings of the 2005 Interna
- [10] Z. Iqbal, "Self-organizing wireless sensor networks for inter-vehicle communication," Master Thesis, Department of Computer and Electrical Engineering, Halmstad University, 2006.
- [11] J. S. Lee, "System and method for intelligent traffic control using wireless sensor and actuator networks," Patent # 20080238720, 2008.
- [12] S. Edward and A. Hollar, "COTS Dust," Master Thesis, Department of Electrical and Computer Engineering, Berkeley, 2000, Vol. 1, pp. 62.
- [13] S. Y. Cheung, S. Coleri, B. Dunder, S. Ganesh, C. W. Tan, and P. Varaiya, "Traffic measurement and vehicle classification with a single magnetic sensor," University of California, Berkeley, 84th Annual Meeting Transportation Research Board, January 2005, Washington, D.C.
- [14] Swedish National Road and Transportation Research Institute, <http://www.vti.se/nordic/1-0mapp/100sv2.html>.