

# HARDWARE IMPLEMENTATION OF ENTROPY ENCODER USING $\Psi_1, k$ ENCODING SCHEME ON RECONFIGURABLE LOGIC

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**Abstract:** In this paper, hardware implemented a entropy encoder using Rice  $\Psi_1, k$  encoding scheme. The design can calculate the value of  $k$  in real time and then selects the number of pass through bits. The adder used in this design is serial adder, this reduces the resource usage and also reduces the power consumption of the design. The target device to implement the design is Virtex 5 FPGA (XC5VLX20T-2FF232). Xilinx XST is used to synthesize the design and it is coded in VHDL. The synthesis report shows that 2% of slice registers, 5% of Slice LUTs and 8% of slices were occupied by this design, this suggests area requirement.

**Keywords:** Rice algorithm,  $\Psi_1, k$ , Entropy Encoding, FPGA

## I. INTRODUCTION

Real-time lossless compression hardware will be a part of next generation computing chips (very large scale integrated circuits, VLSI) to sustain higher data rates over on-board limited channel and storage capacities. They include processor, network, and storage chips. With a reduced number of bits, limited capacity of transmission channels or storage can be used effectively. Such a reduction has a direct impact on complexity reductions, cost reductions, as well as overall system reliability improvements [1]. Image communication and storage are examples of applications that benefit from image compression, because the compression results in (i) faster (real-time) image transmission through band limited channels and (ii) lower requirements for storage space. Non compressed images require many data bits, making it impossible for real-time transmission through band limited channels—such as 48 kbit per second (kbps) and 112 kbps integrated services digital network (ISDN), as well as 9.6 kbps voice-grade telephone or radio channels [1]. For example, transmitting a 256×256 pixels grayscale still-image over the voice-grade line would require at least 54.61 s. Furthermore, one HDTV format needs 60 frames of 1280×720 pixels per second. Using 24 bpp colour pixels, this HDTV format would require an impractical channel capacity of 1,440 Mbps. For example, space explorations by National Aeronautics and Space Administration (NASA) missions generate huge science data, requiring real-time compression [2]. Consequently, international bodies such as Committee for Space Data Systems (CCDS) have defined compression standards for real-time systems [3].

## II. COUNTER CODE ALGORITHM

To design the architecture, we must first understand the counter code algorithm and then use it as a design

requirement. A basic counter coder called  $\Psi_1$  (or sometimes also called PSI-1) works as follows [2]:

Given a block of data samples (for  $j = 1, \dots, J$ ), coder  $\Psi_1$  assumes that each sample takes a symbol  $s_i$ , for  $i = 1, \dots, 256$ , as shown in Table 1. Coder  $\Psi_1$  treats each sample symbol  $S_i$  having sample data  $d_i$  as a non-negative integer number  $x_i$ . The average length of sample data is  $R = 8$  bits per sample.

For every sample in the block (having a symbol  $s_i$ , thus having sample data  $d_i$ ), a  $\Psi_1$  encoder converts  $d_i$  into a codeword  $w_i$  of a length  $l_i = X_i + 1$ , consisting of  $x_i$  consecutive zero bits '0' followed by a closing one bit '1' (see again Table 1). For example, if a sample happens to be  $d_i = 0000\ 0011$ , it must have  $x_i = 3$ , and the  $\Psi_1$  then encodes it using 4 bits, i.e., 3 zeros followed by a one. Hence, the encoding algorithm (converting  $d_i$  into  $w_i$ ) is simply down counting, which is summarized in Table 1.

The reconstruction is obviously simple counting too. Given a codeword  $w_i$ , a  $\Psi_1$  decoder just counts the number of zero bits until a one appears. The counting result is the sample value  $x_i$ . Using Table 1, it determines that the codeword belongs to a symbol  $s_i$ , hence it produces the sample data  $d_i$  as its output.

We then propose to use the counter coder as an alternative and more computationally efficient entropy coder. One basic counter coder called  $\Psi_1$  (or PSI-1) works as follows [2]. Given a block of data samples (for  $j = 1, \dots, J$ ),  $\Psi_1$  replaces every sample in the block with a number of consecutive zero bits '0' followed by a closing one bit '1' (see Table 1). For example, if a sample happens to have a value of 55, the  $\Psi_1$  encodes it using 56 bits, i.e., 55 zeros followed by a one. Hence, the encoding algorithm is simple. The reconstruction is obviously simple too. A  $\Psi_1$  decoder just counts the number of zero bits until a one appears. The counting result is the sample value.

Define now a function  $i(j)$  such that a particular data block consists of symbols  $\{S_{i(1)}, S_{i(2)}, \dots, S_{i(j)}\}$ . The total number of bits required to encode a data block is (for index  $j$  and block size  $J$ )

$$L = J + \sum_{j=1}^J X_{i(j)} \dots \dots \dots (1)$$

Notice that this code basically allocates more codeword bits to data samples with higher sample values, i.e.  $X_i \geq X_j \Leftrightarrow l_i \geq l_j$ . This means  $\Psi_1$  code is optimal if the statistical distribution of data samples is monotonically decreasing, i.e.,  $X_i \geq X_j \Leftrightarrow P(S_i) \geq P(S_j)$ . The average codeword length of  $\Psi_1$  code is:

$$R = \sum_{i=1}^q (P(s_i) i) \dots \dots \dots (2)$$

It has been studied elsewhere [3] that this code is optimal for a (monotonically decreasing distribution) source with a first-order entropy around 1, i.e.,  $1.5 < H < 2.5$ . It should be clear that in a monotonically decreasing distribution, the probability of a sample has a large value is low. As a result, the probability of long codeword length Eq. (11) is low. Thus it is optimal. We say that range is the natural entropy range of  $\Psi_1$ . For sources with entropies outside that range, there are several variations of  $\Psi_1$ .

For example, if  $H > 2.5$ , it is safe to assume that the LSBs of sample data  $di(j)$  are completely random. In this case there is no need to perform any compression on those LSBs. We can then split  $di(j)$  into two portions:  $k$  LSBs and  $(8-k)$  MSBs. The MSBs are coded using  $\Psi_1$  code before being sent to bitstream, while the LSBs are sent uncoded. A decoder first recovers the MSBs using  $\Psi_1$  decoder, and then concatenates the results with the uncoded LSBs, resulting in the desired  $di(j)$ . It can be shown that this approach has a natural entropy range  $1.5 + k < H < 2.5 + k$ . This code is called  $\Psi_{1,k}$ .

Table 1: Code Word of input data

i	Symbol Si	Sample Xi	Sample Data di	Codeword Wi	Length Li
1	S1	0	0000 0000	1	1
2	S2	1	0000 0001	01	2
3	S3	2	0000 0010	001	3
4	S4	3	0000 0011	0001	4
..	...	...	...	...	...
25	S256	255	1111 1111	0000...	256
6				01	

For  $0.75 < H < 1.5$  range, we can first use the  $\Psi_1$ , resulting in a bitstream with many '1' bits. To exploit this, we can cascade it using another simple code. The simple code first complements the results of  $\Psi_1$  (i.e., converting '0' into '1' and vice versa), and group the resulting bit into binary 3-tuples. It finally codes each binary 3-tuples in a way that a tuple with many '0' bits will use short codewords. This code is called  $\Psi_0$ .

For sources with entropy  $H < 0.75$ , we can cascade the coder with another coder, such as ZRL coder described above. A ZRL encoder processes samples, and provides its outputs to a counter coder. In effect the ZRL coder brings the data entropy into counter code natural range.

Figure 1 shows the flow chart of  $\Psi_{1,k}$  encoder.

### III. HARDWARE IMPLEMENTATION

#### A. Data Path Structure

It has been studied elsewhere that the  $\Psi_1$  code discussed in chapter 1 is optimal for monotonically decreasing distribution source with first order entropies outside this, Rice introduced a concept of word splitting. If  $H > 2.5$ , it is safe to assume that the LSBs of the sample data  $di(j)$  are completely random. In this case there is no need to perform compression on those LSBs. An encoder can split data  $di(j)$  into two parts:  $k$  LSBs and  $8-k$  MSBs as shown in figure 2.

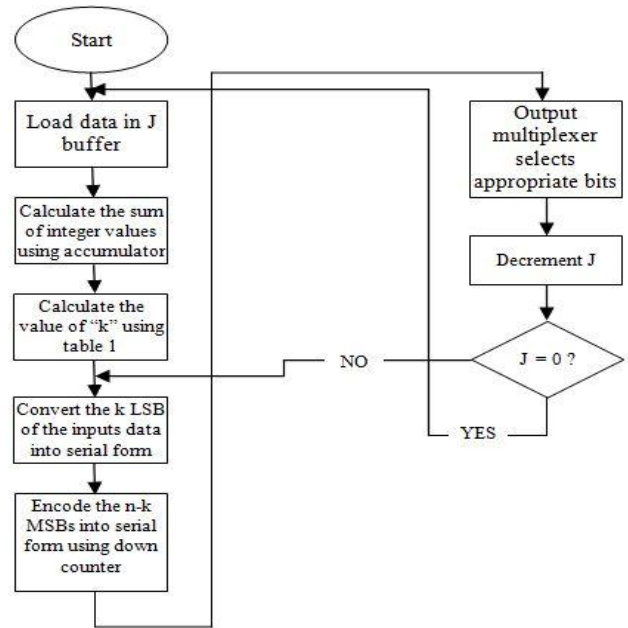


Figure 1: Flow Chart –  $\Psi_{1,k}$

The MSBs are encoded using  $\Psi_1$  coder before being sent to output bit stream. While the LSBs are sent uncoded (or said to encoded using  $\Psi_1 - 3$ ). At the receiver the decoder concatenates the data received.

This counter compression of word splitting is called  $\Psi_{1,k}$ , the entropy range of this enhanced encoder is  $1.5 + k < H < 2.5 + k$ . The  $\Psi_{1,k}$  encoder is shown in figure 4.2. Now a mechanism of appropriate word splitting is needed at the encoder side.

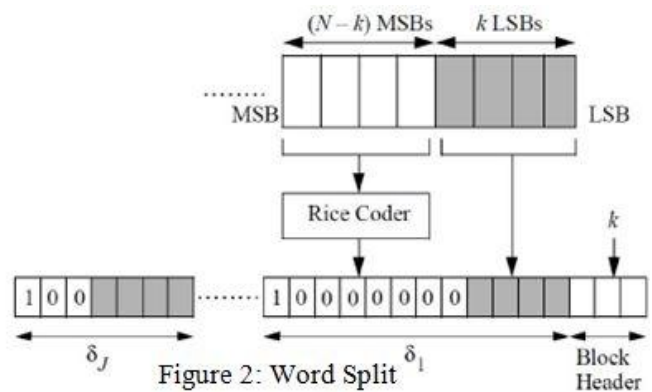


Figure 2: Word Split

#### B. Splitter

Given a block of data samples (for  $j = 1, \dots, J$ ), the  $\Psi_{1,k}$  coder must then have a mechanism to estimate the entropy of the block to ensure it uses the optimal  $k$ . Rice has come with an estimation rule of thumb based on sum of  $x_i$  values in the block [2]. Since we assume that the data samples has a source according to Table 1 with statistics of a monotonically decreasing distribution,  $x_i$  with low values are likely to occur. The lower the entropy, the more the distribution is skewed toward lower value  $x_i$  (i.e., lower  $L$ ). As a result, a block with lower entropy will have a smaller sum of  $x_i$  values in the block. In other words, average entropy in a block can be estimated from  $L / J$ . This rule of thumb is shown in Table 2. A small value of  $L / J$  is reflected in a smaller sum of  $x_i$ , corresponding to a low entropy value,

hence a small selected  $k$ . As mentioned before if the samples do not have such a characteristic, i.e., a nonnegative and monotonically decreasing distribution, there are several simple preprocessing schemes available to preprocess the samples to comply with the characteristics.

Table 2: A rule of thumb to estimate block entropy for  $J = 8$  and  $n = 8$  for 8 options of coders (adapted from [2])

Decision range	Sum of $x_i$ values	Entropy	$k$
$LJ \leq 5/2$	0 – 12	1.5	0
$5/2 < LJ \leq 9/2$	13 – 28	2.5	1
$9/2 < LJ \leq 17/2$	29 – 60	3.5	2
$17/2 < LJ \leq 33/2$	61 – 125	4.5	3
$33/2 < LJ \leq 65/2$	126 – 252	5.5	4
$65/2 < LJ \leq 129/2$	251 – 508	6.5	5
$129/2 < LJ \leq (128n-831)/2$	509 – 764	7.5	6
$(128n-831)/2 < LJ$	765 – 1023	8	8

**C. Proposed Accumulator**

It is observed from the base paper adder design that the adder is not in use for most of the duration, so we can replace the 7 RCA structure by a single RCA structure shown in figure 3.

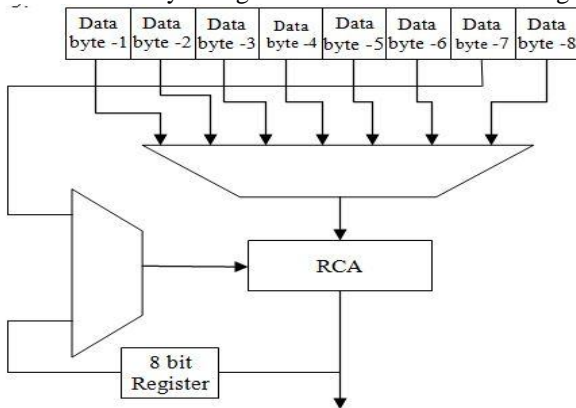


Figure 3: Proposed Accumulator

The proposed adder uses a single RCA, in the first clock cycle the data byte 8 and data byte 7 are added and the result is stored in 8 bit register. In the next clock cycle the data byte 6 is added with the value stored in 8 bit register and so on. This will reduce the area and power consumption of the design.

**D. Selection Logic**

The selection logic splits the input data bytes into two halves,  $k$  LSB bits and  $n-k$  MSBs. The proposed architecture of selection logic is shown in figure 4. The comparator shown in figure 4 compares the value of the sum evaluated from the adder shown in figure 3 with internal reference value mentioned in table 2 in this chapter. Then the appropriate value of  $k$  is found out, then the input data byte is divided into two halves using a multiplexer.

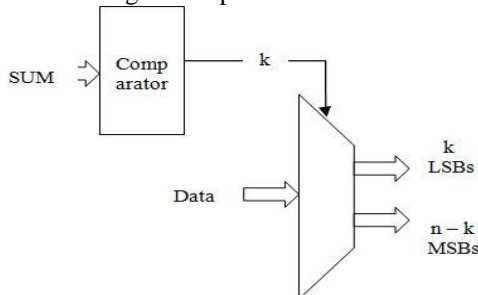


Figure 4: Proposed Selection Logic

**E. MSB Encoder**

The  $n-k$  MSBs encoder is implemented using a simple down counter shown in figure 5.

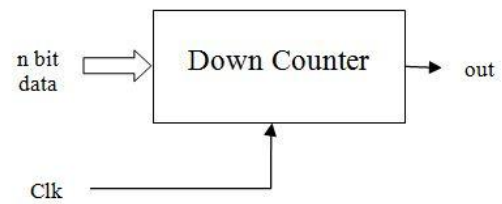


Figure 5: MSB Encoder

The remaining  $n-k$  bits are encoded using the down counter shown in figure 5. The counter has  $n$  bit of input lines, in our case the value of  $n$  is 8, so the input data line is 8 bit wide. The  $n-k$  bit data is appended with  $k$  zeros and the integer value is loaded in the down counter, now at every rising clock pulse the down counter is decremented by one and the output line "out" is kept at zero, when the down counter reaches zero, the output line "out" is made 1. This implements the PSI – 1 encoder in the PSI – 1,  $k$  rice algorithm.

**F. Output Multiplexer**

The output multiplexer connects the encoder with serial bit oriented channel. Figure 6 shows the output multiplexer.

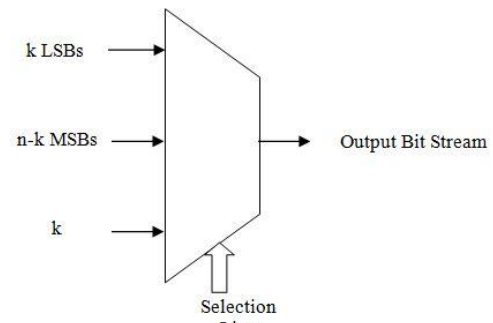


Figure 6: Output Multiplexer

**IV. RESULTS**

Figure 7 shows the simulation of PSI – 1,  $k$  encoder with the transmission value of 4,3,3,3,2,2,2,2.



Figure 7: Simulation of PSI – 1,  $k$  Encoder

Table 3 shows the resource usage of proposed design of PSI – 1,k encoder. We have implemented the design on Virtex 5 FPGA device.

Table 3: Resource Usage Summary

S.no	Resources	Quantity	% use Proposed Design
1	Number of Slice Registers	305	2%
2	Number of Slice LUTs	660	5%
3	Number of occupied Slices	277	8%

Table 4 shows the power consumption summary of proposed PSI – 1,k encoder, Figure 8 shows the characteristics of power consumption with respect to operating frequency.

Table 4: Power Consumption Summary

S.no	Frequency (Mhz)	Static Power Consumption (mW)	Dynamic Power Consumption (mW)	Total Power Consumption (mW)
1	30	321	11	332
2	50	321	14	335
3	80	321	19	340
4	100	321	22	343
5	150	321	30	350
6	200	321	37	358
7	247 (MOF)	321	43	365

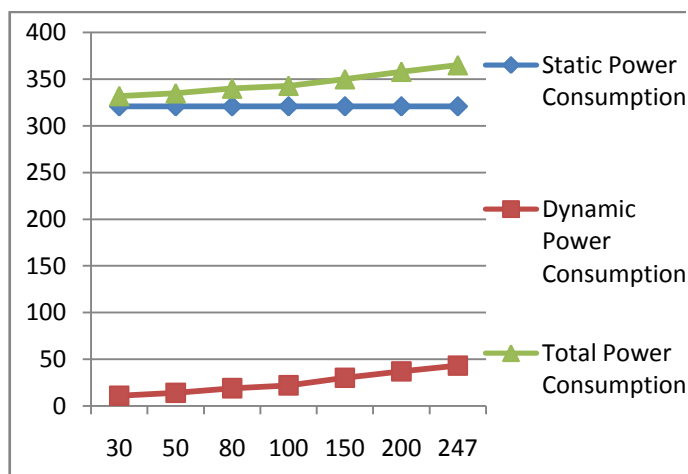


Figure 8: Power Consumption characteristics with frequency

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