

## SIMULATION OF BLACK OUT IN TRANSMISSION NETWORK USING PRIM'S ALGORITHM

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**Abstract:** A graph theory technique called Prim's Algorithm is used to recover the loads after complete black out is proposed here. We have proposed three stages to recover the load. Newton-Raphson based load flow technique is used to find energizing path of power flow technique. In the first stage, we are going to start from Generator of maximum capability (Slack bus). In the second stage, we are going to energize the generators from slack bus. In the third stage, we are going to recover the loads.

**Keywords:** Graph theory, blackout, minimum spanning tree, load flow solution.

### I. INTRODUCTION

Power system is a complex network involving the flow of power, which is generated using various techniques to meet the need of the industries or domestic consumers [1]. A brownout is an intentional drop in voltage in an electrical power supply system used for load reduction in an emergency [7]. A voltage reduction may be an effect of disruption of an electrical grid, or may occasionally be imposed in an effort to reduce load and prevent a blackout [9].

### II. LOAD FLOW ANALYSIS

Power flow studies are of great importance in planning & designing the future expansion of power system as well as in determining the best operation of existing systems [2]. The principle information obtained from power flow study is the magnitude & phase angle of voltage at each bus the real & reactive power following in each line [3]. Power flow calculations usually employ iterative techniques such as Newton-Raphson method solves the polar form of power flow equations until  $\Delta P$  &  $\Delta Q$  mismatches at all buses fall within specified tolerances [8]. Newton's method is a successive approximation procedure based on initial estimate of the unknown and the use of Taylor's series expansion and the terms are limited to first order approximation [4]. LF Newton is developed for solution of power flow problems by Newton Raphson method [5].

### III. GRAPH THEORY

Graph theory is a branch of data structures concerned about how the networks can be encoded & their properties measured [6]. A graph (G) is a set of points called vertices & the lines connecting the points called Edges. The graphs are broadly classified into two types It differs from a directed graph as each edge in E is an unordered pair of vertices. If

(v, w) is an undirected edge then (v, w) = (w, v). The other classification is weighted & unweights graphs. Here electrical network is analyzed as an undirected & weighted graph.

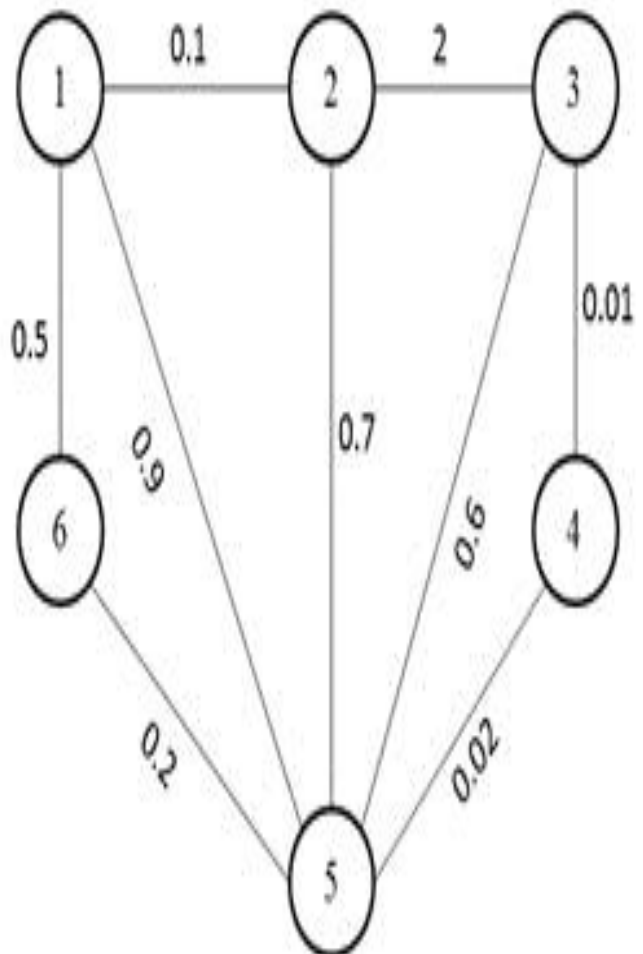


Fig. 1: Example Problem

### IV. PRIM'S ALGORITHM

Prim's algorithm, conceived by Dutch computer scientist Robert C. Prim in 1957, is a graph search algorithm that solves the single-source shortest path problem for a graph with nonnegative edge path costs, producing a shortest path tree [6]. It can also be used for finding costs of shortest paths from a single vertex to a single destination vertex by stopping the algorithm once the shortest path to the

destination vertex has been determined.

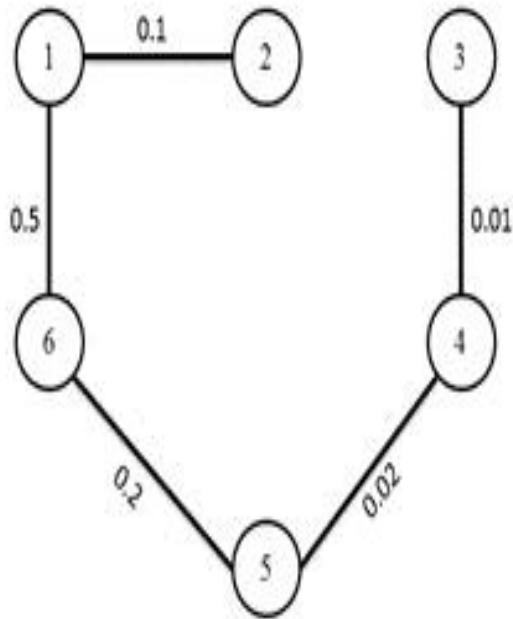


Fig. 2: Minimum Spanning Tree by Prim's Algorithm

By applying Prim's Algorithm we get minimum spanning tree of distance 0.83.

TABLE. I: Comparison of Results of Various Algorithms

ALGORITHM	DISTANCE CALCULATED FROM MINIMUM SPANNING TREE
Prim's Algorithm	0.83
Dijkstra's Algorithm	1.03
Kruskal's Algorithm	1.03
Reverse Delete Algorithm	1.03

V. RECOVERY PROCESS

The whole recovery process is divided into 3 stages:

A. Black Start

Due to any critical fault or transient in the network a complete blackout will be occurring.

B. System Reconstruction

The generator (Slack bus) started first & based on the sequence of starting & starting time the generators on the network are started.

C. Load Recovery

Initially the critical loads are fed & later after stabilization of

the critical loads all other loads are connected.

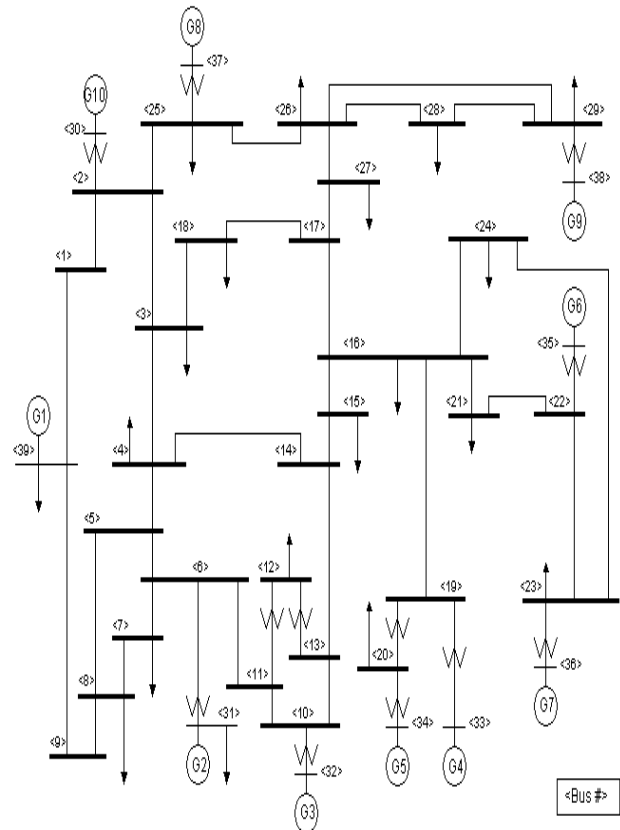


Fig. 3: Initial Network

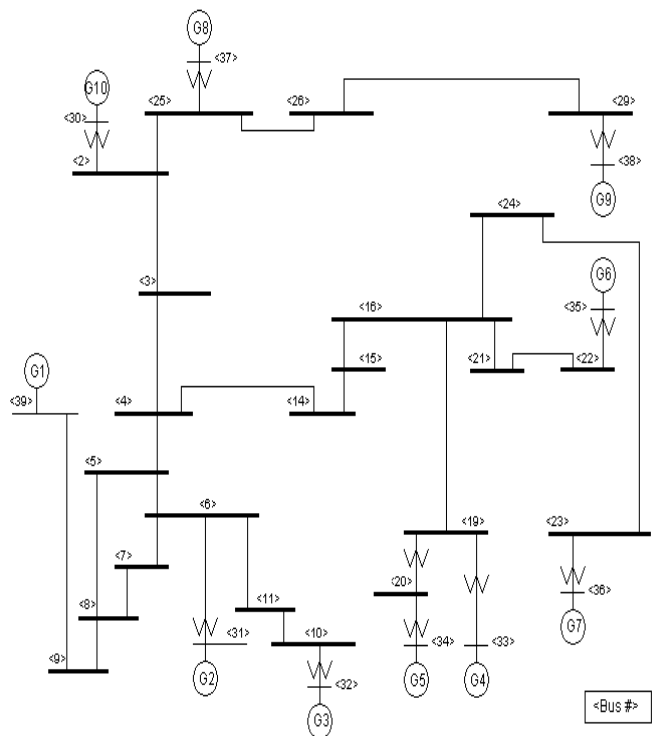


Fig. 4: System Reconstruction Stage

TABLE. II: Bus Data of Initial Network

Bus No	Bus Code	Voltage	Load		Generator	
			MW	Mvar	MW	Mvar
1	0	1	0	0	0	0
2	0	1	0	0	0	0
3	0	1	322	2.4	0	0
4	0	1	500	184	0	0
5	0	1	0	0	0	0
6	0	1	0	0	0	0
7	0	1	233.8	84	0	0
8	0	1	522	176	0	0
9	0	1	0	0	0	0
10	0	1	0	0	0	0
11	0	1	0	0	0	0
12	0	1	7.5	88	0	0
13	0	1	0	0	0	0
14	0	1	0	0	0	0
15	0	1	320	153	0	0
16	0	1	329	32.3	0	0
17	0	1	0	0	0	0
18	0	1	158	30	0	0
19	0	1	0	0	0	0
20	0	1	628	103	0	0
21	0	1	274	115	0	0
22	0	1	0	0	0	0
23	0	1	247.5	84.6	0	0
24	0	1	308.6	-92	0	0
25	0	1	224	47.2	0	0
26	0	1	139	17	0	0
27	0	1	281	75.5	0	0
28	0	1	206	27.6	0	0
29	0	1	283.5	26.9	0	0
30	2	1	0	0	250	0
31	1	1	9.2	4.6	0	0
32	2	1	0	0	650	0
33	2	1	0	0	632	0
34	2	1	0	0	508	0
35	2	1	0	0	650	0
36	2	1	0	0	560	0
37	2	1	0	0	540	0
38	2	1	0	0	830	0
39	2	1	1104	250	1000	0

TABLE. III: Output of Initial Network

Load	Generation	Injected
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MW	Mvar	MW	Mva	Mvar
6097	1409	6145	1445.9	0

Total Line loss	
MW	Mvar
48.310	36.862

TABLE. IV: Detailed Output of Initial Network

Bus no	Voltage	Angle	Load		Generation		Injected
			MW	Mvar	MW	Mvar	
1	1.004	-8.408	0	0	0	0	0
2	0.985	-5.3	0	0	0	0	0
3	0.966	-8.525	322	2.4	0	0	0
4	0.944	-9.657	500	184	0	0	0
5	0.95	-8.525	0	0	0	0	0
6	0.953	-7.782	0	0	0	0	0
7	0.942	-10.22	233	84	0	0	0
8	0.942	-10.77	522	176	0	0	0
9	0.988	-10.47	0	0	0	0	0
10	0.962	-4.966	0	0	0	0	0
11	0.958	-5.922	0	0	0	0	0
12	0.937	-5.876	7.5	88	0	0	0
13	0.957	-5.712	0	0	0	0	0
14	0.951	-7.457	0	0	0	0	0
15	0.947	-7.538	320	153	0	0	0
16	0.961	-7.538	329	32.3	0	0	0
17	0.965	-5.752	0	0	0	0	0
18	0.964	-8.098	158	30	0	0	0
19	0.979	0.195	0	0	0	0	0
20	0.976	-0.81	628	103	0	0	0
21	0.959	-2.97	274	115	0	0	0
22	0.976	2.178	0	0	0	0	0
23	0.973	1.939	247	84.6	0	0	0
24	0.967	-5.612	308	-92	0	0	0
25	0.996	-3.796	224	47.2	0	0	0
26	0.987	-5.072	139	17	0	0	0
27	0.97	-7.291	281	75.5	0	0	0
28	0.989	-1.128	206	27.6	0	0	0
29	0.992	1.96	283	26.9	0	0	0
30	1	-2.668	0	0	250	87.2	0
31	1	0	9.2	4.6	525	227.	0
32	1	2.801	0	0	650	234.	0
33	1	5.394	0	0	632	141.	0
34	1	4.497	0	0	508	133	0
35	1	7.64	0	0	650	195	0
36	1	10.907	0	0	560	133	0
37	1	3.416	0	0	540	336	0
38	1	9.433	0	0	830	65.8	0
39	1	-10.19	110	250	100	190	0

VI. RESULTS OF NEWTON-RAPHSON METHOD						14	-7.388	-33.942	34.737	0.007	-32.872
						16	-312.612	-119.058	334.516	1.106	-4.022
--Line--	Power at bus & line flow			--Line loss--							
From To	MW	Mvar	MVA	MW	Mvar						
1	0.000	0.000	0.000			16		-329.000	-32.300	330.582	
2	-125.392	24.820	127.824	0.671	-61.246	15	313.718	115.036	334.144	1.106	-4.022
39	125.392	-24.820	127.824	0.158	-71.359	17	230.494	-60.279	238.246	0.425	-7.052
						19	-502.095	-35.931	503.379	4.372	24.659
2	0.000	0.000	0.000			21	-328.465	35.266	330.353	0.953	-7.401
1	126.063	-86.066	152.640	0.671	-61.246	24	-42.651	-86.392	96.347	0.028	-5.761
3	363.659	94.209	375.664	1.924	-2.131	17	0.000	0.000	0.000		
25	-239.722	66.443	248.759	4.534	-8.760	16	-230.070	53.226	236.147	0.425	-7.052
30	-250.000	-74.586	260.889	0.000	12.691	18	208.966	-6.651	209.072	0.328	-8.420
						27	21.104	-46.575	51.134	0.020	-29.845
3		-322.000	-2.400	322.009		18		-158.000	-30.000	160.823	
2	-361.736	-96.340	374.345	1.924	-2.131	3	50.638	-28.231	57.976	0.034	-19.479
4	90.339	85.188	124.170	0.241	-16.229	17	-208.638	-1.769	208.645	0.328	-8.420
18	-50.603	8.752	51.355	0.034	-19.479	19	0.000	0.000	0.000		
4		-500.000	-184.000	532.781		16	506.468	60.590	510.079	4.372	24.659
3	-90.098	-101.416	135.657	0.241	-16.229	33	-629.063	-82.369	634.433	2.937	59.579
5	-140.702	-43.228	147.193	0.190	-8.983	20	122.595	21.779	124.515	0.113	2.230
14	-269.200	-39.356	272.062	0.661	-1.741	34	-505.518	-83.451	512.360	2.482	49.640
5	0.000	0.000	0.000			19	-122.482	-19.549	124.032	0.113	2.230
4	140.892	34.245	144.995	0.190	-8.983	21		-274.000	-115.000	297.155	
6	-457.407	-77.875	463.988	0.476	2.265	16	329.418	-42.667	332.170	0.953	-7.401
8	316.514	43.629	319.507	0.911	-0.462	22	-603.418	-72.333	607.738	3.202	32.014
6	0.000	0.000	0.000			21	0.000	0.000	0.000		
5	457.883	80.139	464.843	0.476	2.265	21	606.620	104.347	615.529	3.202	32.014
7	420.738	84.670	429.173	1.223	8.594	23	43.380	25.408	50.273	0.019	-17.229
11	-362.412	-21.029	363.021	1.014	-0.800	35	-650.000	-129.755	662.825	0.000	65.891
31	-516.210	-143.780	535.859	0.000	79.029	22	-247.500	-84.600	261.560		
7		-233.800	-84.000	248.432		22	43.380	25.408	50.273	0.019	-17.229
6	-419.516	-76.076	426.358	1.223	8.594	23	-247.500	-84.600	261.560		
8	185.716	-7.924	185.885	0.155	-5.140	22	-43.361	-42.636	60.811	0.019	-17.229
8		-522.000	-176.000	550.872		24	354.204	1.205	354.206	2.924	12.573
5	-315.604	-44.092	318.669	0.911	-0.462	36	-558.343	-43.168	560.009	1.657	90.132
7	-185.560	2.784	185.581	0.155	-5.140	24		-308.600	92.000	322.022	
9	-20.836	-134.692	136.294	0.371	-29.592	16	42.680	80.631	91.230	0.028	-5.761
9	0.000	0.000	0.000			23	-351.280	11.369	351.464	2.924	12.573
8	21.207	105.100	107.218	0.371	-29.592	25		-224.000	-47.200	228.919	
39	-21.207	-105.100	107.218	0.027	-117.899	2	244.256	-75.204	255.571	4.534	-8.760
10	0.000	0.000	0.000			26	69.987	-3.567	70.078	0.173	-48.698
11	364.020	65.127	369.800	0.593	-0.339	37	-538.242	31.571	539.168	1.758	67.958
13	285.980	73.760	295.339	0.379	-2.637	26		-139.000	-17.000	140.036	
32	-650.000	-138.887	664.673	0.000	95.486	25	-69.813	-45.131	83.131	0.173	-48.698
11	0.000	0.000	0.000			27	261.018	80.848	273.252	1.102	-11.383
6	363.425	20.229	363.988	1.014	-0.800	28	-140.507	-24.706	142.663	0.879	-66.490
10	-363.427	-65.466	369.276	0.593	-0.339	29	-189.697	-28.011	191.754	2.134	-77.314
12	0.001	45.237	45.237	0.036	0.971	27		-281.000	-75.500	290.966	
12	-7.500	-88.000	88.319			17	-21.084	16.731	26.915	0.020	-29.845
11	0.034	-44.266	44.266	0.036	0.971	26	-259.916	-92.231	275.795	1.102	-11.383
13	-7.534	-43.734	44.379	0.036	0.976	28		-206.000	-27.600	207.841	
13	0.000	0.000	0.000			26	141.386	-41.784	147.431	0.879	-66.490
10	-285.601	-76.397	295.642	0.379	-2.637	29	-347.386	14.184	347.676	1.737	-5.691
14	278.031	31.687	279.830	0.774	-6.998	29		-283.500	-26.900	284.773	
12	7.570	44.710	45.347	0.036	0.976	26	191.831	-49.304	198.066	2.134	-77.314
14	0.000	0.000	0.000			28	349.123	-19.874	349.688	1.737	-5.691
4	269.861	37.615	272.470	0.661	-1.741	38	-824.454	42.278	825.537	5.546	108.145
13	-277.256	-38.685	279.942	0.774	-6.998	30		250.000	87.276	264.796	
15	7.395	1.070	7.472	0.007	-32.872	2	250.000	87.277	264.797	0.000	12.691
15	-320.000	-153.000	354.696			<b>Total loss</b>		<b>48.310</b>			<b>36.862</b>

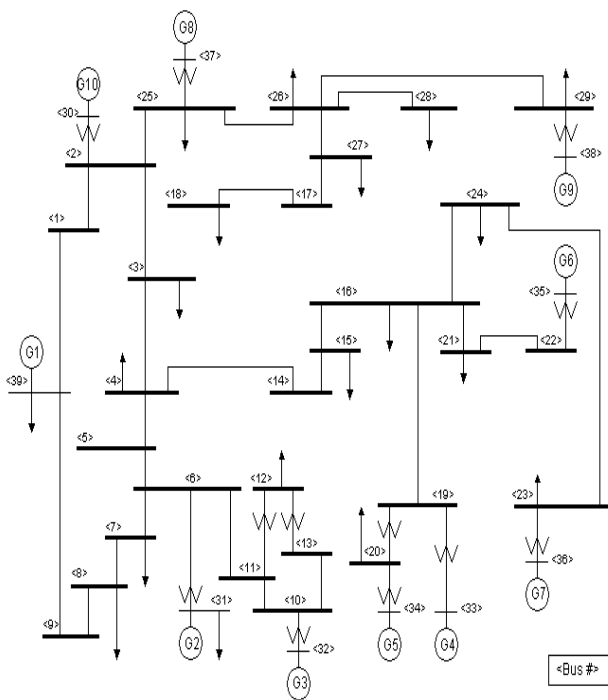


Fig. 5: Load Recovery Stage

## VII. CONCLUSION

This paper presents the use of Prim's Algorithm for service restoration plan after a complete blackout by application of graph theory the process had been made simple and user friendly. In order to demonstrate the efficiency of prim's algorithm it has been applied to IEEE 10 Generator 39 Bus System. We carry out three stages of recovery process by using dijkstra's algorithm. Newton-Raphson method is used to carry out load flow analysis. The simulation results show that Newton-Raphson method is effective and promising. It has been found that by application of prim's algorithm the transmission losses can be reduced to significant extent. The advantages are (1) solution procedure leads to the optimum solution & (2) avoid combinational explosion of the number of the number of configurations to be tested. This it is believed that the results from Prim's algorithm in power system restoration results in better plan, so it can be considered for real time application. Since the simulation implementation is done only for 39 bus system it can be extended to networks with more number of buses.

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